CS380: Computer Graphics Viewing Transformation

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Course URL: http://sglab.kaist.ac.kr/~sungeui/CG/

Class Objectives (Ch. 7)

- **Know camera setup parameters**
- **Understand viewing and projection processes**

Viewing Transformations

- **Map points from world spaces to eye space**
	- **Can be composed from rotations and translations**

Viewing Transformations

- **Goal: specify position and orientation of our camera**
	- **Defines a coordinate frame for eye space**

"Framing" the Picture

● **A new camera coordinate**

- **Camera position at the origin**
- **Z-axis aligned with the view direction**
- **Y-axis aligned with the up direction**

● **More natural to think of camera as an object positioned in the world frame**

Viewing Steps

● **Rotate to align the two coordinate frames and, then, translate to move world space origin to camera's origin**

An Intuitive Specification

● **Specify three quantities:**

- Eye point (e)
-
- **the image** →
- **Eye point (e) - position of the camera**
- **Look-at point (p) - center of the image**
- Up-vector (μ_a) will be oriented upwards in

Deriving the Viewing Transformation

● **First compute the look-at vector and normalize**l $\mathsf{I} = \mathsf{p} - \mathsf{e}$ \rightarrow l $I=\frac{1}{12}$ \rightarrow ˆ

● **Compute right vector and normalize**

 $\vec{r} = \vec{l} \times \vec{u}_a$ $=$ 1 \times

● **Perpendicular to the look-at and up vectors** \rightarrow

r

 $\hat{\mathsf{r}} = \frac{\mathsf{r}}{\mathsf{r}}$

ˆ \blacksquare

● **Compute up vector**

- **•** \vec{u}_a is only approximate direction
- **Perpendicular to right and look-at vectors**

$$
\hat{\mathbf{u}} = \hat{\mathbf{r}} \times \hat{\mathbf{l}}
$$

Rotation Component

● **Map our vectors to the cartesian coordinate axes**

$$
\begin{bmatrix} 1 & 0 & 0 \ 0 & 1 & 0 \ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} \hat{r} & \hat{u} & -\hat{i} \end{bmatrix} R_v
$$

- To compute R_v we invert the matrix on the right
	- ● **This matrix M is orthonormal (or orthogonal) – its rows are orthonormal basis vectors: vectors mutually orthogonal and of unit length**

• Then,
$$
M^{-1} = M^{T}
$$

\n• So,
\n
$$
\mathbf{R}_{v} = \begin{bmatrix} \hat{\mathbf{r}}^{t} \\ \hat{\mathbf{u}}^{t} \\ -\hat{\mathbf{l}}^{t} \end{bmatrix}
$$

Translation Component

- **The rotation that we just derived is specified about the eye point in world space**
	- ● **Need to translate all world-space coordinates so that the eye point is at the origin**

 ν \neg $-e$

● **Composing these transformations gives our viewing transform,** V *t t* $W = e$ **K l** : $\dot{\mathcal{W}}^{\prime}=\dot{\boldsymbol{\mathcal{e}}}^{\mathrm{\scriptscriptstyle T}}\mathbf{R}_{\mathrm{\scriptscriptstyle W}}\mathbf{T}_{\mathrm{\scriptscriptstyle T}}$

$$
\mathbf{V} = \mathbf{R}_{\nu} \mathbf{T}_{-e} = \begin{bmatrix} \hat{r}_{x} & \hat{r}_{y} & \hat{r}_{z} & 0 \\ \hat{u}_{x} & \hat{u}_{y} & \hat{u}_{z} & 0 \\ -\hat{l}_{x} & -\hat{l}_{y} & -\hat{l}_{z} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & -e_{x} \\ 0 & 1 & 0 & -e_{y} \\ 0 & 0 & 1 & -e_{z} \\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} \hat{r} & -\hat{r} \cdot \vec{e} \\ \hat{u} & -\hat{u} \cdot \vec{e} \\ -\hat{l} & \hat{l} \cdot \vec{e} \\ 0 & 0 & 0 & 1 \end{bmatrix}
$$

Transform a world-space point into a point in the eye-space

Viewing Transform in OpenGL

● **OpenGL utility (glu) library provides a viewing transformation function:**

gluLookAt (double eyex, double eyey, double eyez, double centerx, double centery, double centerz, double upx, double upy, double upz)

● **Computes the same transformation that we derived and composes it with the current matrix**

Example in the Skeleton Codes of PA2

```
void setCamera () 
{ …
// initialize camera frame transformsfor (i=0; i < cameraCount; i++ )
  {
   double* c = cameras[i];
   wld2cam.push_back(FrameXform());
   glPushMatrix();
   glLoadIdentity();
   gluLookAt(c[0],c[1],c[2], c[3],c[4],c[5], c[6],c[7],c[8]);
   glGetDoublev( GL_MODELVIEW_MATRIX, wld2cam[i].matrix() );
   glPopMatrix();
   cam2wld.push_back(wld2cam[i].inverse());
  }
….}KAIST
```
Projections

● **Map 3D points in eye space to 2D points in image space**

- **Two common methods**
	- **Orthographic projection**
	- ●**Perspective projection**

Orthographic Projection

● **Projects points along lines parallel to z-axis**

- **Also called parallel projection**
- **Used for top and side views in drafting and modeling applications**
- **Appears unnatural due to lack of perspective foreshortening**

Notice that the parallel lines of the tiled floor remain parallel after orthographic projection!

Orthographic Projection

● **The projection matrix for orthographic projection is very simple**

$$
\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}
$$

● **Next step is to convert points to NDC**

View Volume and Normalized Device Coordinates

- **Define a view volume**
- **Compose projection with a scale and a translation that maps eye coordinates to normalized device coordinates**

Orthographic Projections to NDC

Scale the z coordinate in exactly the same way .Technically, this coordinate is not part of the projection. But, we will use this value of z for other purposes

Some sanity checks:

$$
x = left \Rightarrow x' = \frac{2 \cdot left}{right - left} - \frac{right + left}{right - left} = -\frac{right - left}{right - left} = -1
$$

$$
x = right \Rightarrow x' = \frac{2 \cdot right}{right - left} - \frac{right + left}{right - left} = \frac{right - left}{right - left} = 1
$$

Orthographic Projection in OpenGL

● **This matrix is constructed by the following OpenGL call:**

void glOrtho(double left, double right, double bottom, double top, double near, double far);

● **2D version (another GL utility function):**

void gluOrtho2D(double left, GLdouble right, double bottom, GLdouble top);

, which is just a call to glOrtho() with near = -1 and far = 1

Perspective Projection

- **Artists (Donatello, Brunelleschi, Durer, and Da Vinci) during the renaissance discovered the importance of perspective for making images appear realistic**
- **Perspective causes objects nearer to the viewer to appear larger than the same object would appear farther away**
- ●**Homogenous coordinates allow perspective projections using**

linear operators

Signs of Perspective

● **Lines in projective space always intersect at a point**

Perspective Projection

$$
y_s = d\frac{y}{z}
$$

Perspective Projection Matrix

● **The simplest transform for perspective projection is:**

$$
\begin{bmatrix} wx' \\ wy' \\ wz' \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}
$$

- **We divide by w to make the fourth coordinate 1**
	- ●**In this example, w = z**
	- ●**Therefore,** $x' = x / z$ **,** $y' = y / z$ **,** $z' = 0$

Normalized Perspective

● **As in the orthographic case, we map to normalized device coordinates**

NDC Perspective Matrix

● **The values of left, right, top, and bottom are specified at the near depth. Let's try some sanity checks:**

NDC Perspective Matrix

● **The values of left, right, top, and bottom are specified at the near depth. Let's try some sanity checks:**

$$
z = far \Rightarrow z' = \frac{far \frac{far + near}{far - near} + \frac{-2 \cdot far \cdot near}{far - near}}{far} = \frac{\frac{far (far - near)}{far - near}}{\frac{far}{far}} = 1
$$

$$
z = near \Rightarrow z' = \frac{near \frac{far + near}{far - near} + \frac{-2 \cdot far \cdot near}{far - near}}{near} = \frac{\frac{near (near - far)}{far - near}}{\frac{far - near}{ear}} = -1
$$

Perspective in OpenGL

● **OpenGL provides the following function to define perspective transformations:**

> **void glFrustum(double left, double right, double bottom, double top, double near, double far);**

● **Some think that using glFrustum() is nonintuitive. So OpenGL provides a function with simpler, but less general capabilities**

void gluPerspective(double vertfov, double aspect, double near, double far);

gluPerspective()

gluPerspective()

Example in the Skeleton Codes of PA2

```
void reshape( int w, int h)
{
 width = w; height = h;
 glViewport(0, 0, width, height);
```

```
glMatrixMode(GL_PROJECTION); // Select The Projection Matrix
glLoadIdentity(); // Reset The Projection Matrix
// Define perspective projection frustum
double aspect = width/double(height);
```

```
gluPerspective(45, aspect, 1, 1024);
glMatrixMode(GL_MODELVIEW); // Select The Modelview Matrix
```

```
}
```
glLoadIdentity(); // Reset The Projection Matrix

Class Objectives were:

- **Know camera setup parameters**
- **Understand viewing and projection processes**

Homework

● **Suggested reading:**

● **Ch. 12, "Data Structure for Graphics"**

- **Watch SIGGRAPH Videos**
- **Go over the next lecture slides**

PA3

- **PA2: perform the transformation at the modeling space**
- **PA3: perform the transformation at the viewing space**

Next Time

● **Interaction**

