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# CS380: Computer Graphics

# Texture Mapping

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**Course URL:**  
<http://sglab.kaist.ac.kr/~sungeui/CG>

**KAIST**



# Class Objectives (CH. 11)

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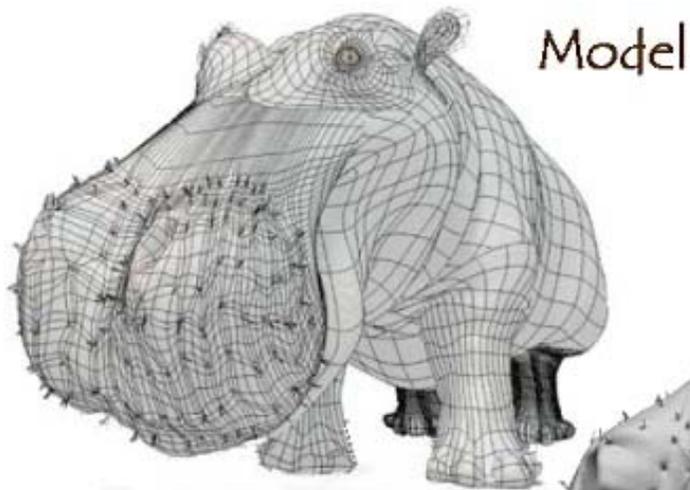
- **Texture mapping overview**
- **Texture filtering**
- **Various applications of texture mapping**

# Texture Mapping

- Requires lots of geometry to fully represent complex shapes of models
- Add details with image representations



# The Quest for Visual Realism



Model + Shading



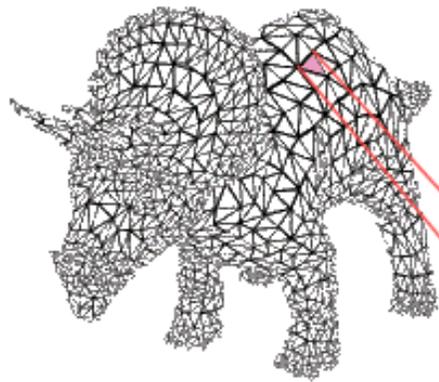
Model + Shading  
+ Textures



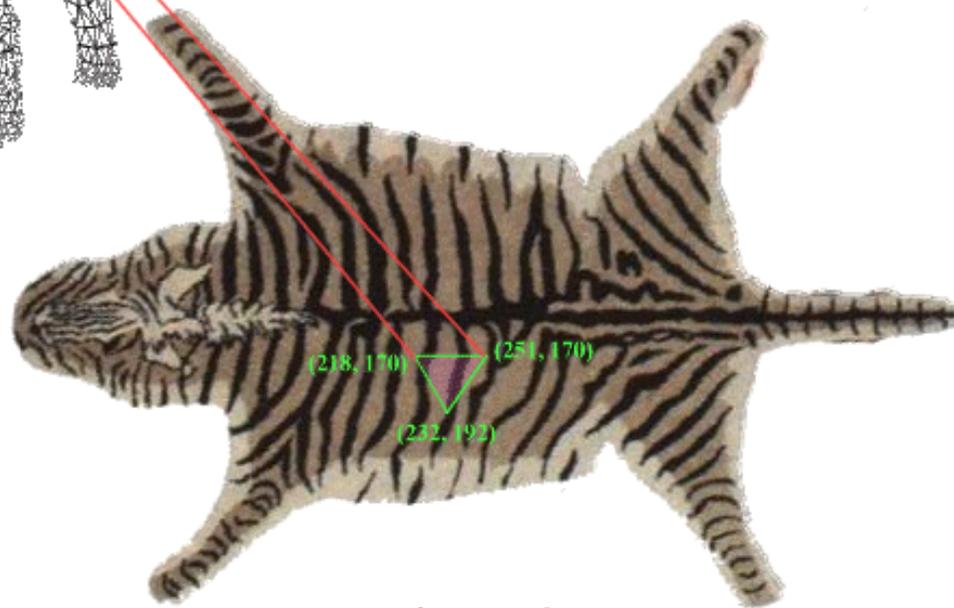
At what point  
do things start  
looking real?

For more info on the computer artwork of Jeremy Birn  
see <http://www.3drender.com/jbirn/productions.html>

# Photo-Textures

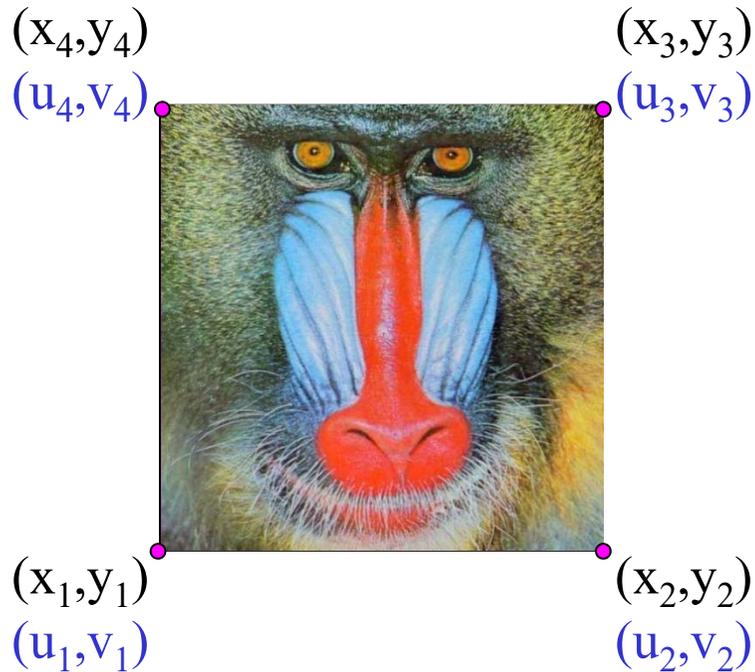


*For each triangle in the model  
establish a corresponding region  
in the phototexture*



*During rasterization interpolate the  
coordinate indices into the texture map*

# Texture Maps in OpenGL



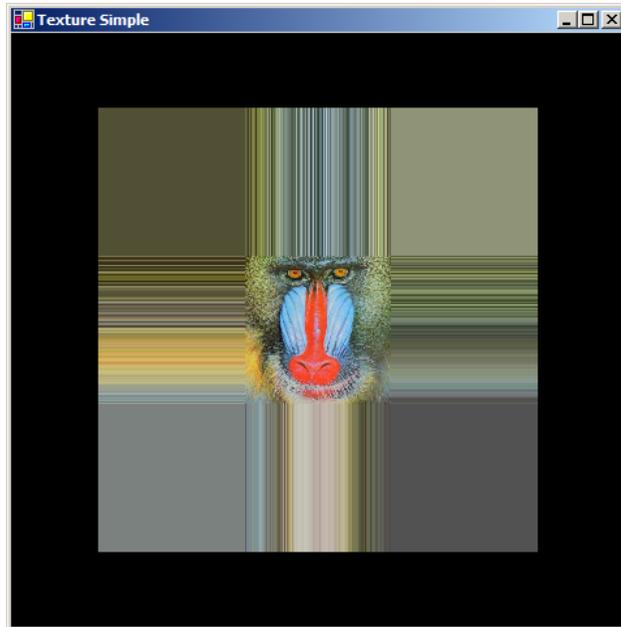
- Specify normalized texture coordinates at each of the vertices  $(u, v)$
- Texel indices  $(s, t) = (u, v) \cdot (\text{width}, \text{height})$

```
glBindTexture(GL_TEXTURE_2D, texID)
glBegin(GL_POLYGON)
    glTexCoord2d(0,1); glVertex2d(-1,-1);
    glTexCoord2d(1,1); glVertex2d( 1,-1);
    glTexCoord2d(1,0); glVertex2d( 1, 1);
    glTexCoord2d(0,0); glVertex2d(-1, 1);
glEnd()
```

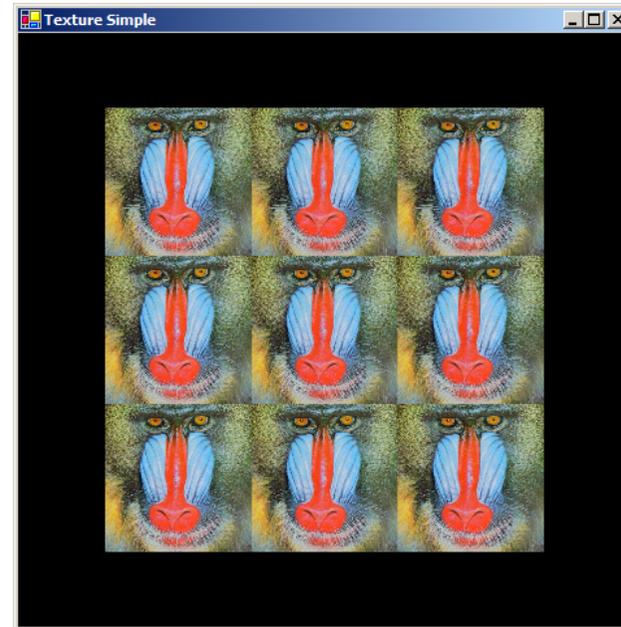
# Wrapping

- The behavior of texture coordinates outside of the range  $[0,1)$  is determined by the texture wrap options.

```
glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_WRAP_S, wrap_mode )  
glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_WRAP_T, wrap_mode )
```



GL\_CLAMP

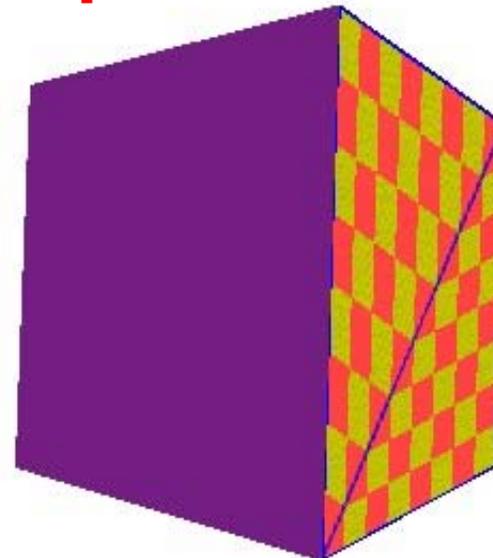
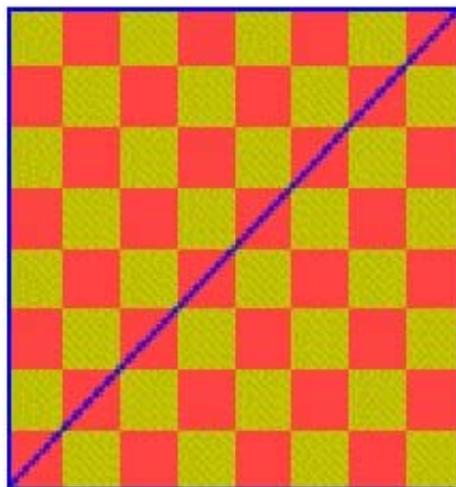


GL\_REPEAT

# Linear Interpolation of Texture Coordinates

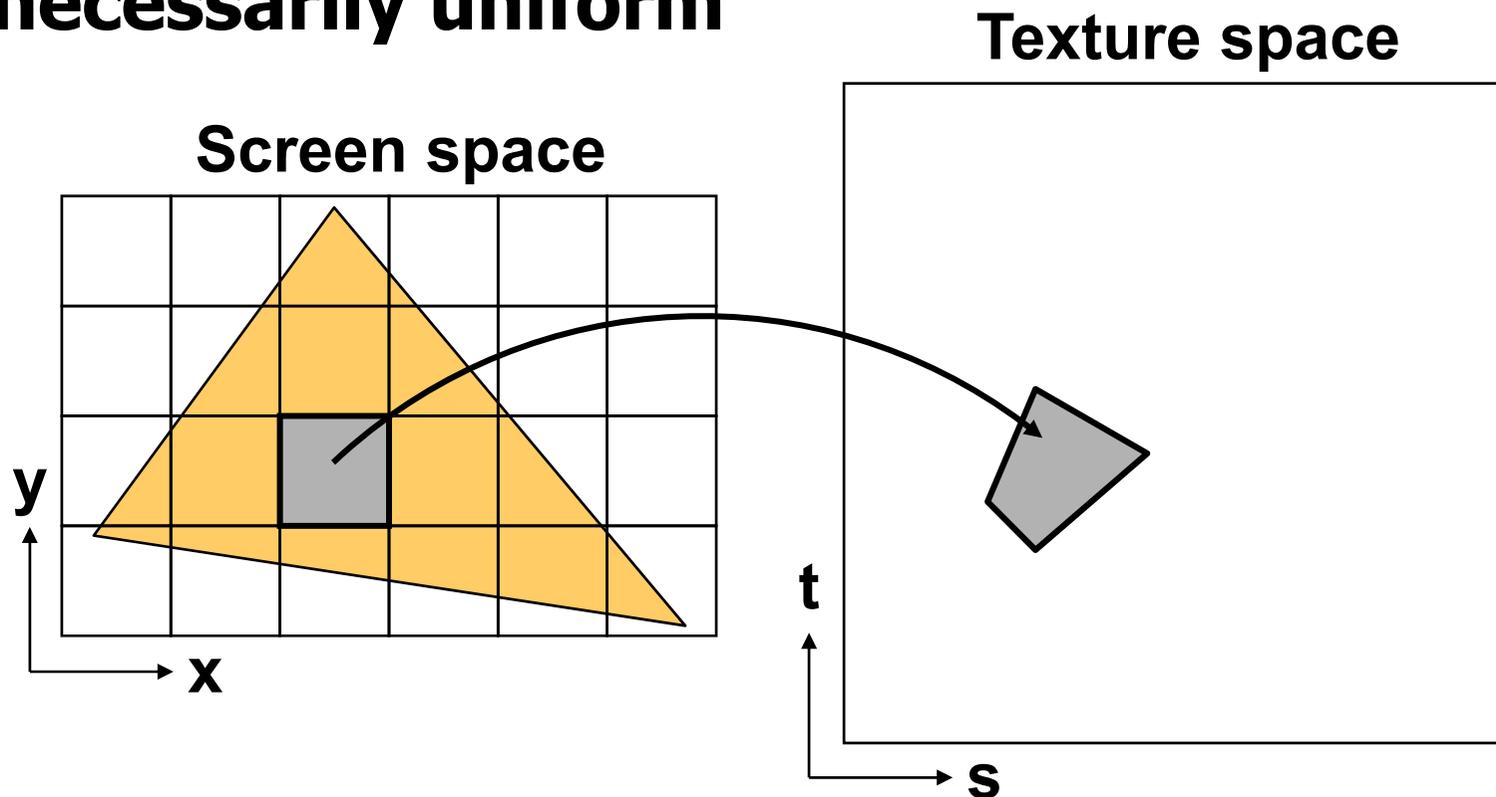
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- **Simple linear interpolation of  $u$  and  $v$  over a triangle in a screen space leads to unexpected results**
  - **Distorted when the triangle's vertices do not have the same depth**
  - **Perspective-correct interpolation (interpolation in the object space) is implemented**



# Sampling Texture Maps

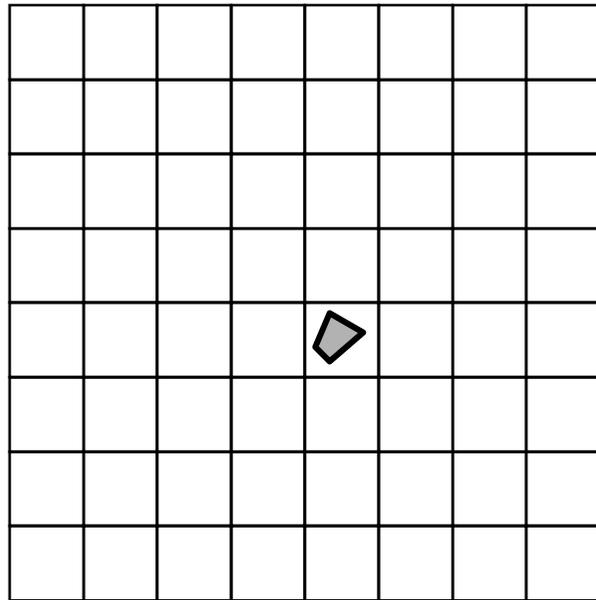
- The uniform sampling pattern in screen space corresponds to some sampling pattern in texture space that is not necessarily uniform



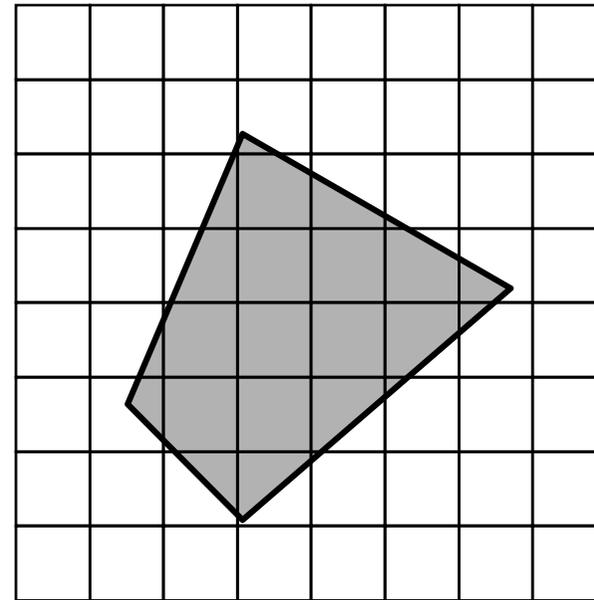
# Sampling Density Mismatch

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- **Sampling density in texture space rarely matches the sample density of the texture itself**

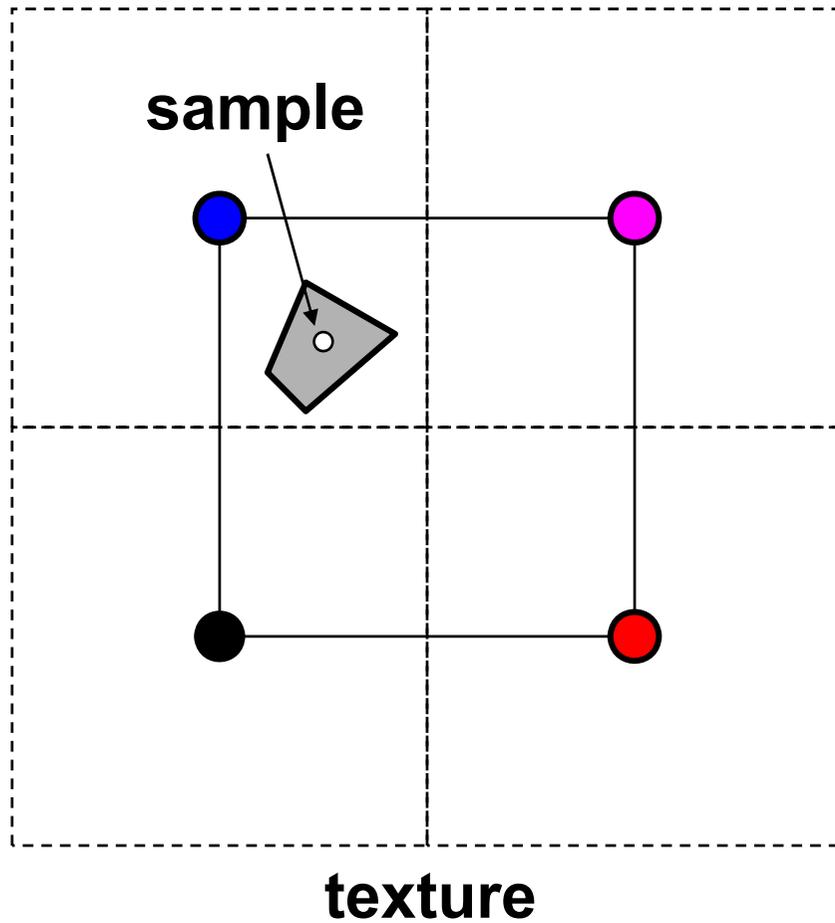


**Oversampling  
(Magnification)**



**Undersampling  
(Minification)**

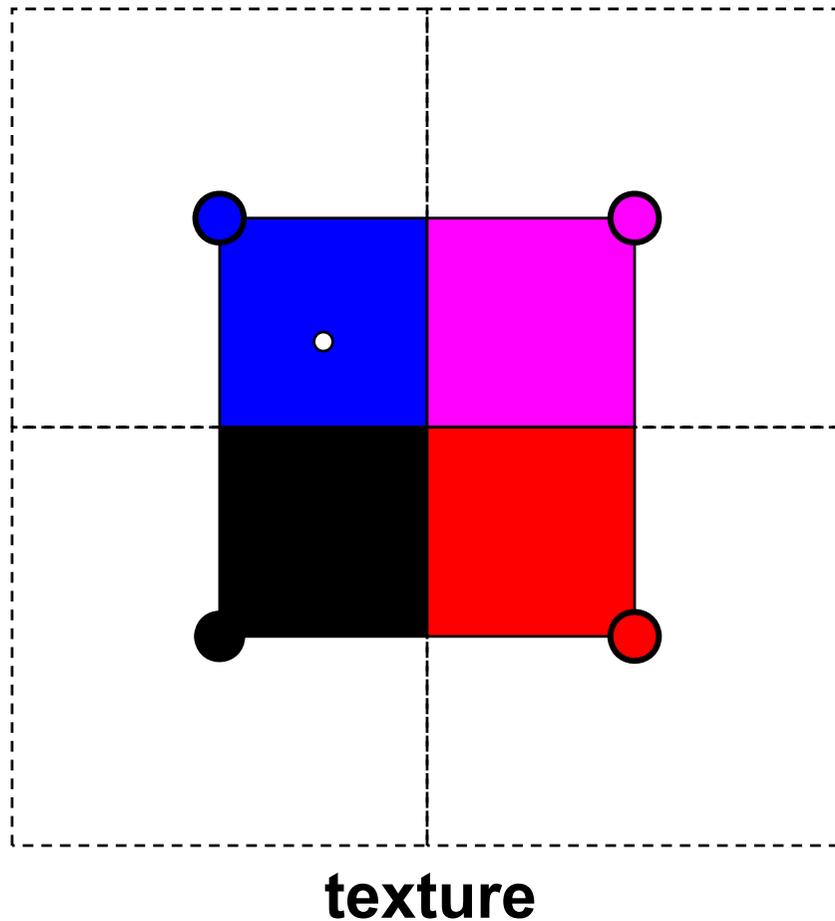
# Handling Oversampling



- How do we compute the color to assign to this sample?

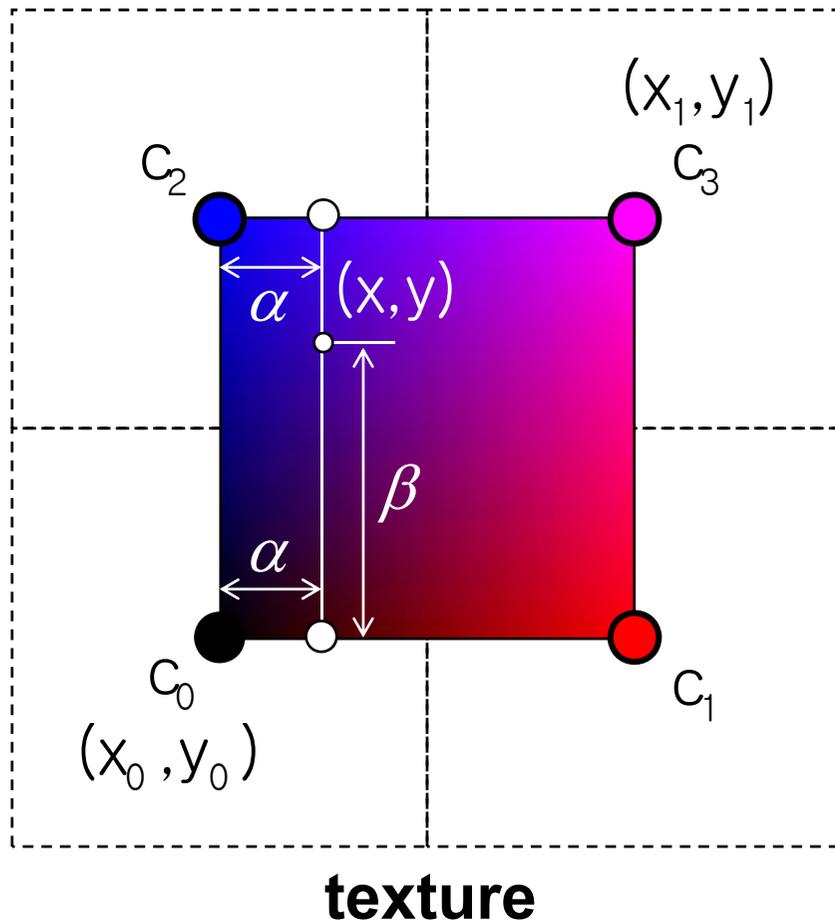
# Handling Oversampling

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- How do we compute the color to assign to this sample?
- Nearest neighbor – take the color of the closest texel

# Handling Oversampling



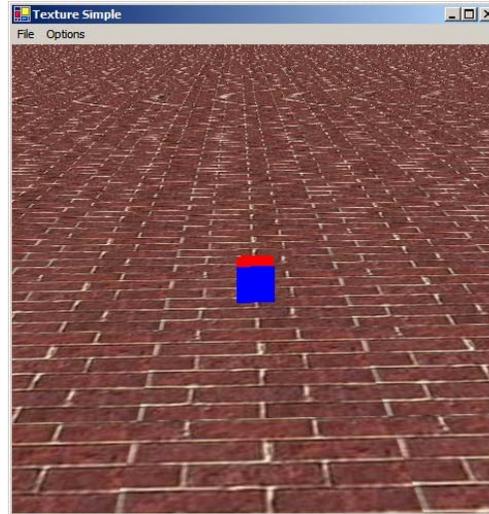
- How do we compute the color to assign to this sample?
- Nearest neighbor – take the color of the closest texel
- Bilinear interpolation

$$\alpha = \frac{x - x_0}{x_1 - x_0} \quad \beta = \frac{y - y_0}{y_1 - y_0}$$

$$c = ((1 - \alpha)c_0 + \alpha c_1)(1 - \beta) + ((1 - \alpha)c_2 + \alpha c_3)\beta$$

# Undersampling

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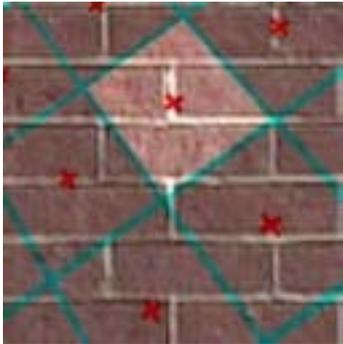


- **Details in the texture tend to pop (disappear and reappear)**
  - **Mortar (white substances) in the brick**
- **High-frequency details lead to strange patterns**
  - **Aliasing**

# Spatial Filtering

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- **To avoid aliasing we need to prefilter the texture to remove high frequencies**
  - Prefiltering is essentially a spatial integration over the texture
  - Integrating on the fly is expensive: perform integration in a pre-process



**Samples and their extents**

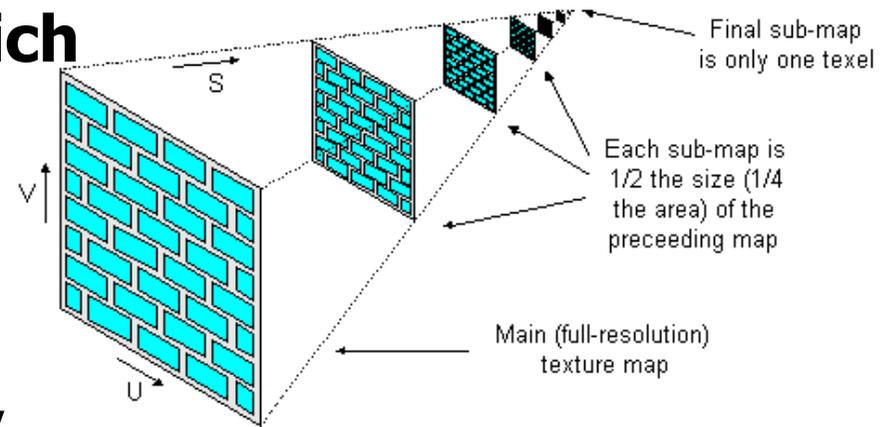


**Proper filtering removes aliasing**

# MIP Mapping

- MIP is an acronym for the Latin phrase *multum in parvo*, which means "many in one place"

- Constructs an *image pyramid*
- Each level is a prefiltered version of the level below resampled at half the frequency

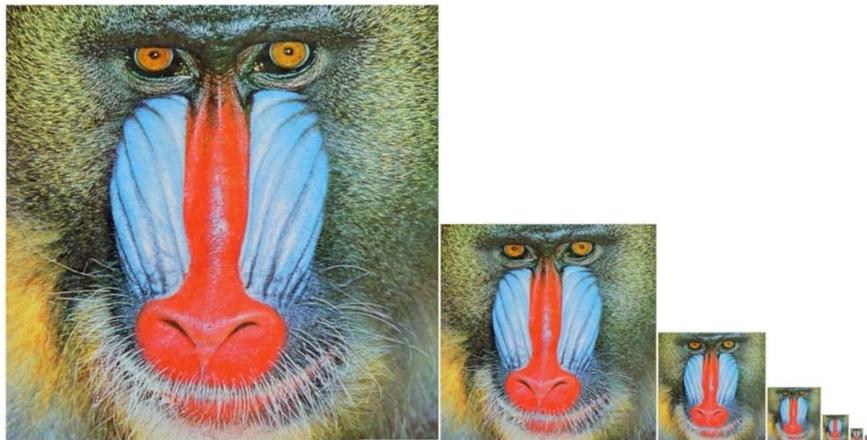


- While rasterizing use the level with the sampling rate closest to the desired sampling rate
  - Can also interpolate between pyramid levels
- How much storage overhead is required?

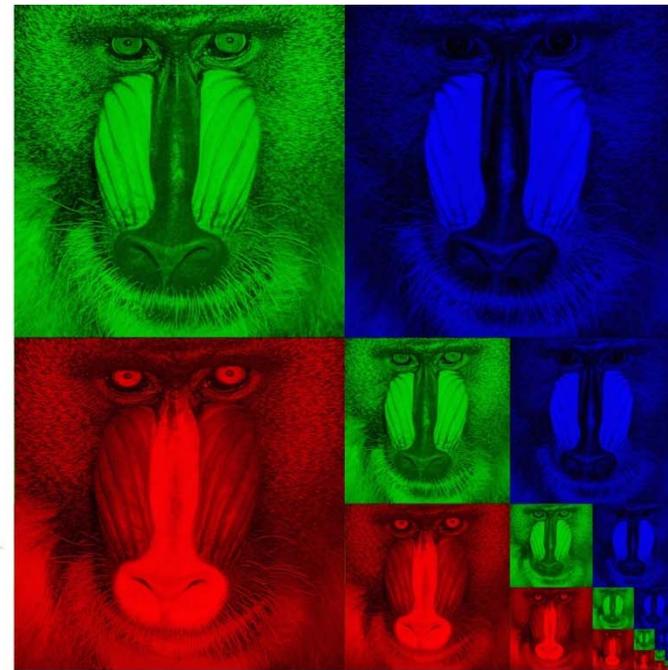
$$\text{mip map size} = \sum_{i=0}^{\infty} \left(\frac{1}{4}\right)^i = \frac{1}{1 - \frac{1}{4}} = \frac{4}{3}$$

# Storing MIP Maps

- One convenient method of storing a MIP map is shown below
  - It also nicely illustrates the 1/3 overhead of maintaining the MIP map



10-level mip map



Memory format of a mip map 

# Finding the MIP Level

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- **Use the projection of a pixel in screen into texture space to figure out which level to use**

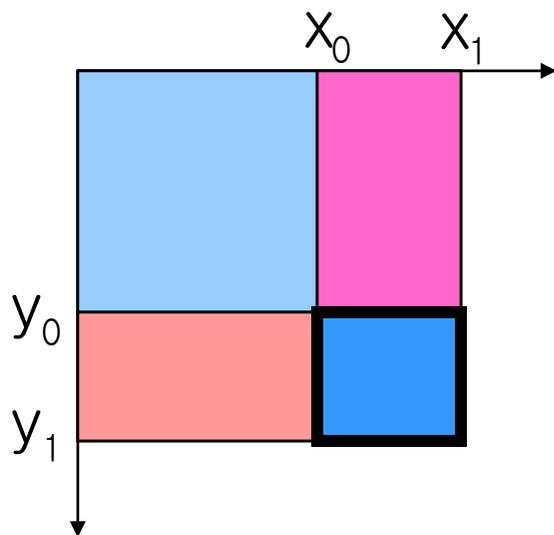
# Summed-Area Tables

- Another way performing the prefiltering integration on the fly
- Each entry in the summed area table is the sum of all entries above and to the left:

1	6	8	3
0	0	3	7
4	7	8	8
5	0	9	9

→

1	7	15	18
1	7	18	28
5	18	37	55
10	23	51	78



What is the sum of the highlighted region?

$$T(x_1, y_1) - T(x_1, y_0) - T(x_0, y_1) + T(x_0, y_0)$$

Divide out area  $(y_1 - y_0)(x_1 - x_0)$

# Summed-Area Tables

- **How much storage does a summed-area table require?**
- **Does it require more or less work per pixel than a MIP map?**
- **Can be implemented in a fragment shader**

No  
Filtering



MIP  
mapping



Summed-  
Area  
Table



# Texture Filtering in OpenGL

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- **Automatic creation**

```
gluBuild2DMipmaps(GL_TEXTURE_2D, GL_RGBA, width, height,  
                 GL_RGBA, GL_UNSIGNED_BYTE, data)
```

- **Filtering**

```
glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_MAG_FILTER, filter )
```

```
glTexParameteri(GL_TEXTURE_2D, GL_TEXTURE_MIN_FILTER, filter )
```

**where filter is:**

GL\_NEAREST

GL\_LINEAR

GL\_LINEAR\_MIPMAP\_LINEAR

GL\_NEAREST\_MIPMAP\_NEAREST

GL\_NEAREST\_MIPMAP\_LINEAR

GL\_LINEAR\_MIPMAP\_NEAREST

inter-level

intra-level

# Uses of Texture Maps

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- **Texture maps are used to add complexity to a scene**
  - **Easier to paint or capture an image than geometry**
- **Model light**
- **Model geometry, etc**

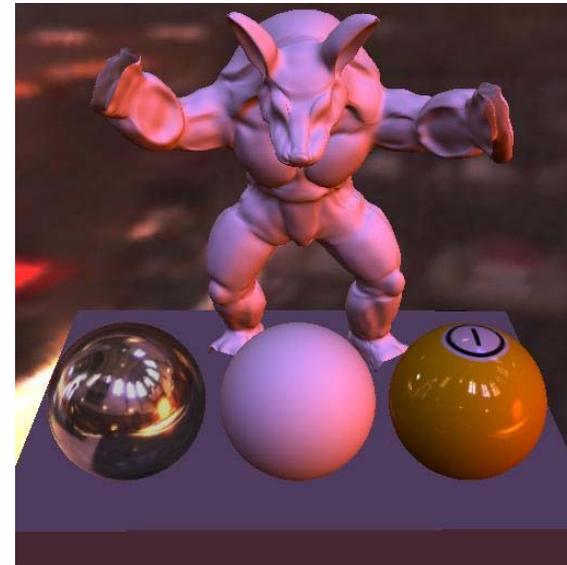


**One of key techniques to overcome various problems of rasterization techniques!**

# Modeling Lighting

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- **Light maps**
  - Supply the lighting directly
  - Good for static environments
- **Projective textures**
  - Can be used to simulate a spot light
  - Shadow maps
- **Environment maps**
  - A representation of the scene around an object
  - Good for reflection

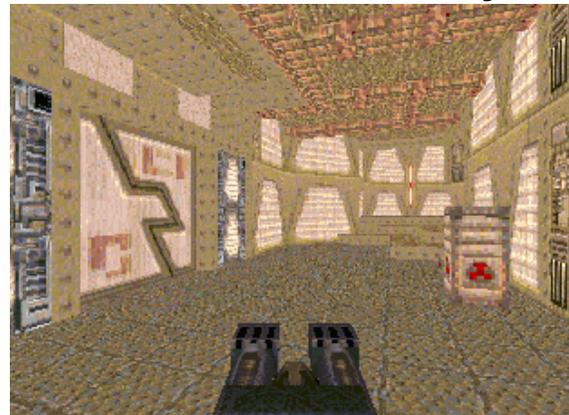


# Light Maps in Quake

- Light maps are used to store pre-computed illumination

	Texture Maps	Light Maps
Data	RGB	Intensity
Resolution	High	Low

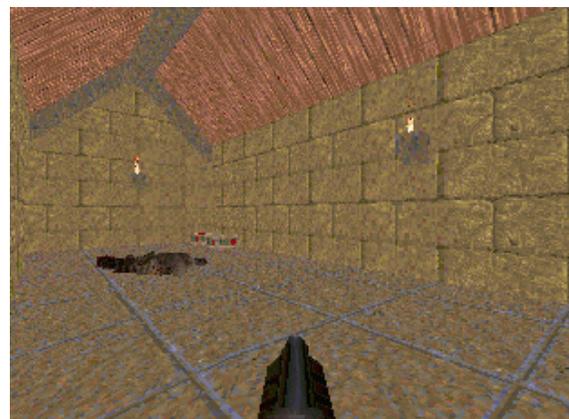
Textures Only



Textures & Light Maps



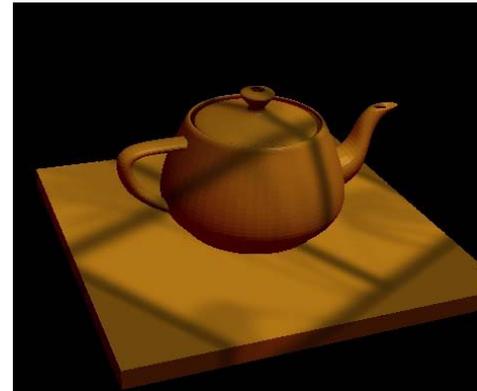
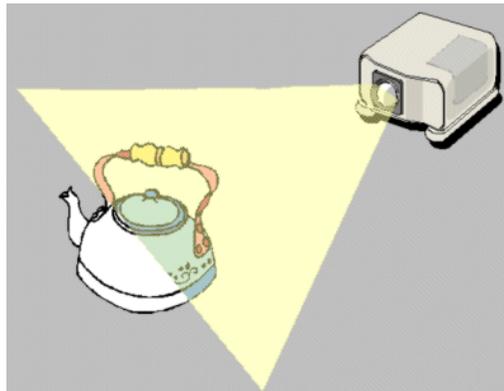
*Light map  
image by Nick  
Chirkov*



# Projective Textures

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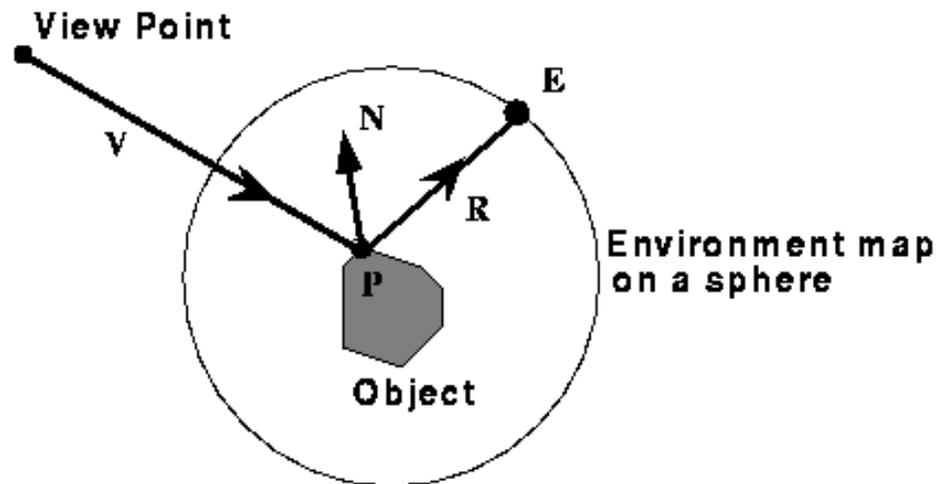
- **Treat the texture as a slide in a projector**
  - A good model for shading variations due to illumination (cool spotlights)
- **Projectors work like cameras in reverse**
  - Camera: color of point in scene  $\rightarrow$  color of corresponding pixel
  - Projector: color of pixel  $\rightarrow$  color of corresponding point in the scene





# Environment Maps

- **Simulate complex mirror-like objects**
  - Use textures to capture environment of objects
  - Use surface normal to compute texture coordinates



# Environment Maps - Example

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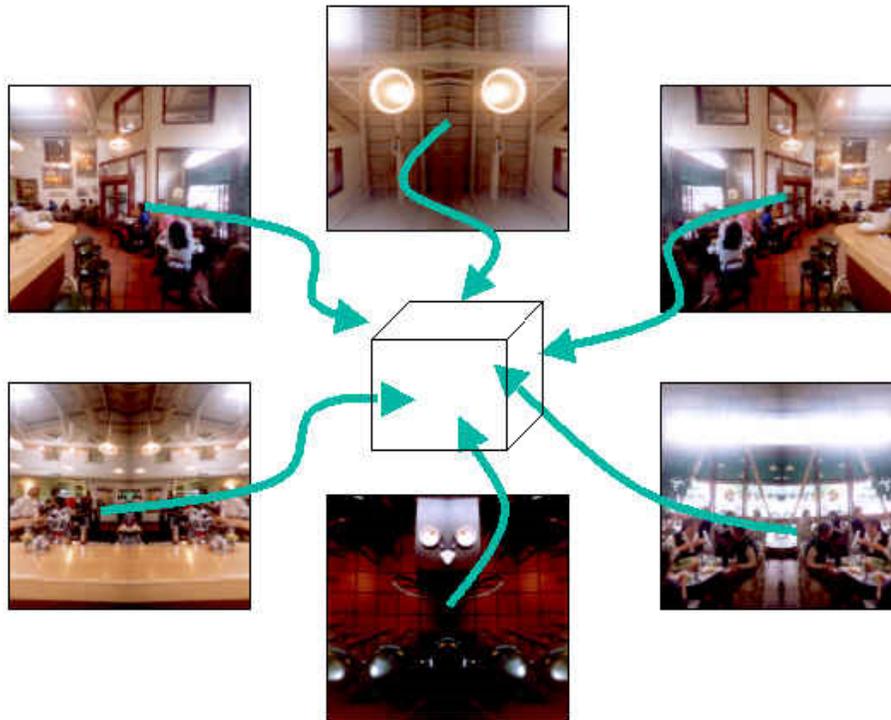


**T1000 in Terminator 2 from Industrial Light and Magic**

# Cube Maps

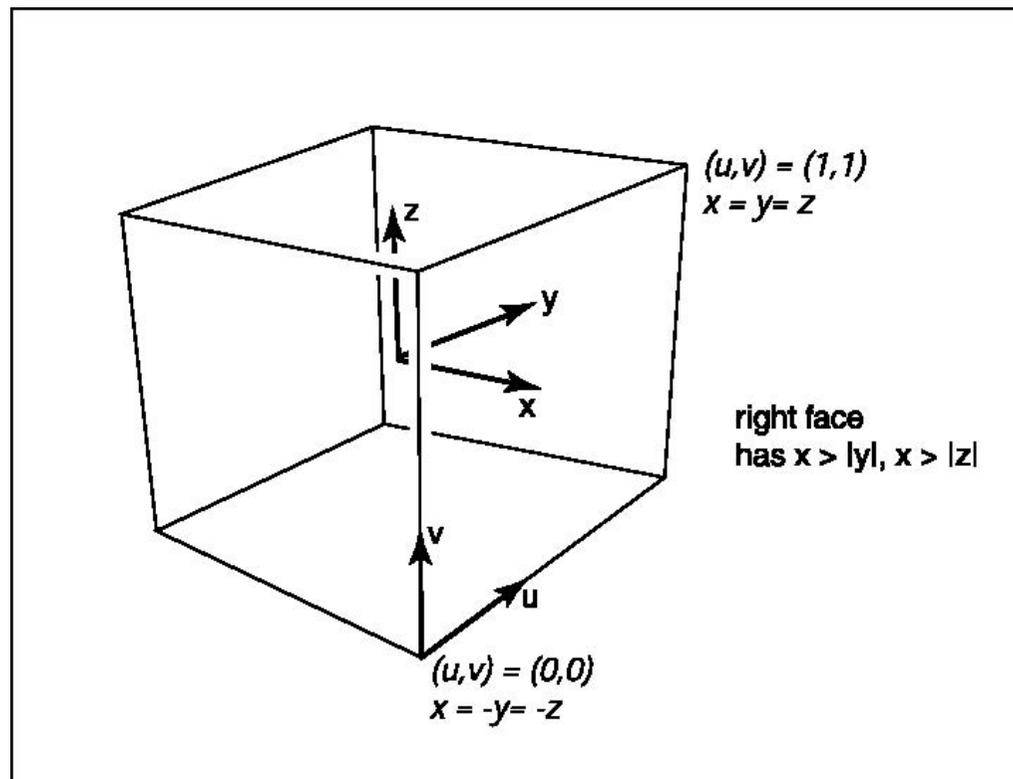
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- **Maps a viewing direction  $\mathbf{b}$  and returns an RGB color**
  - **Use stored texture maps**



# Cube Maps

- Maps a viewing direction  $\mathbf{b}$  and returns an RGB color
  - Assume  $\mathbf{b} = (x, y, z)$ ,



- Identify a face based on magnitude of  $x, y, z$

-For the right face, compute texture coord.  $(u, v)$

$$u = (y+x)/(2x)$$

$$v = (z+x)/(2x)$$

# Environment Maps - Problems

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- **Expensive to update dynamically**
- **Not completely accurate**
  - **One of main reason that Cars (Pixar movie of 2006) used ray tracing**



images from NVIDIA

**Reflection of swimming pool is wrong**

# Environment Maps - Problems

---

- **Expensive to update dynamically**
- **Not completely accurate**
  - **One of main reason that Cars (Pixar movie of 2006) used ray tracing**



# Modeling Geometry

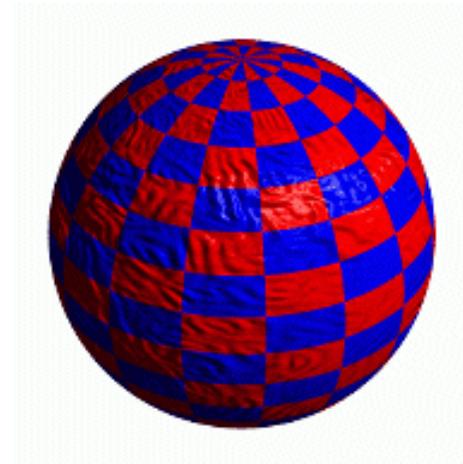
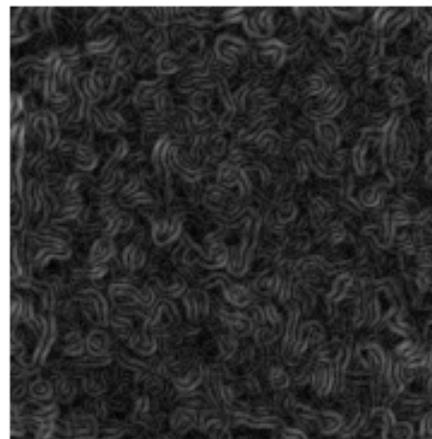
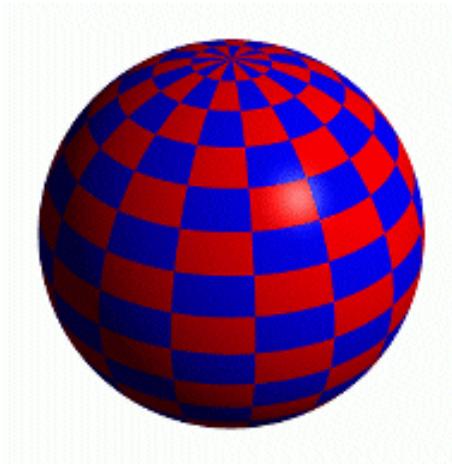
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- **Store complex surface details in a texture rather than modeling them explicitly**
- **Bump maps**
  - Modify the existing normal
- **Normal maps**
  - Replace the existing normal
- **Displacement maps**
  - Modify the geometry
- **Opacity maps and billboards**
  - Knock-out portions of a polygon using the alpha channel

# Bump Mapping

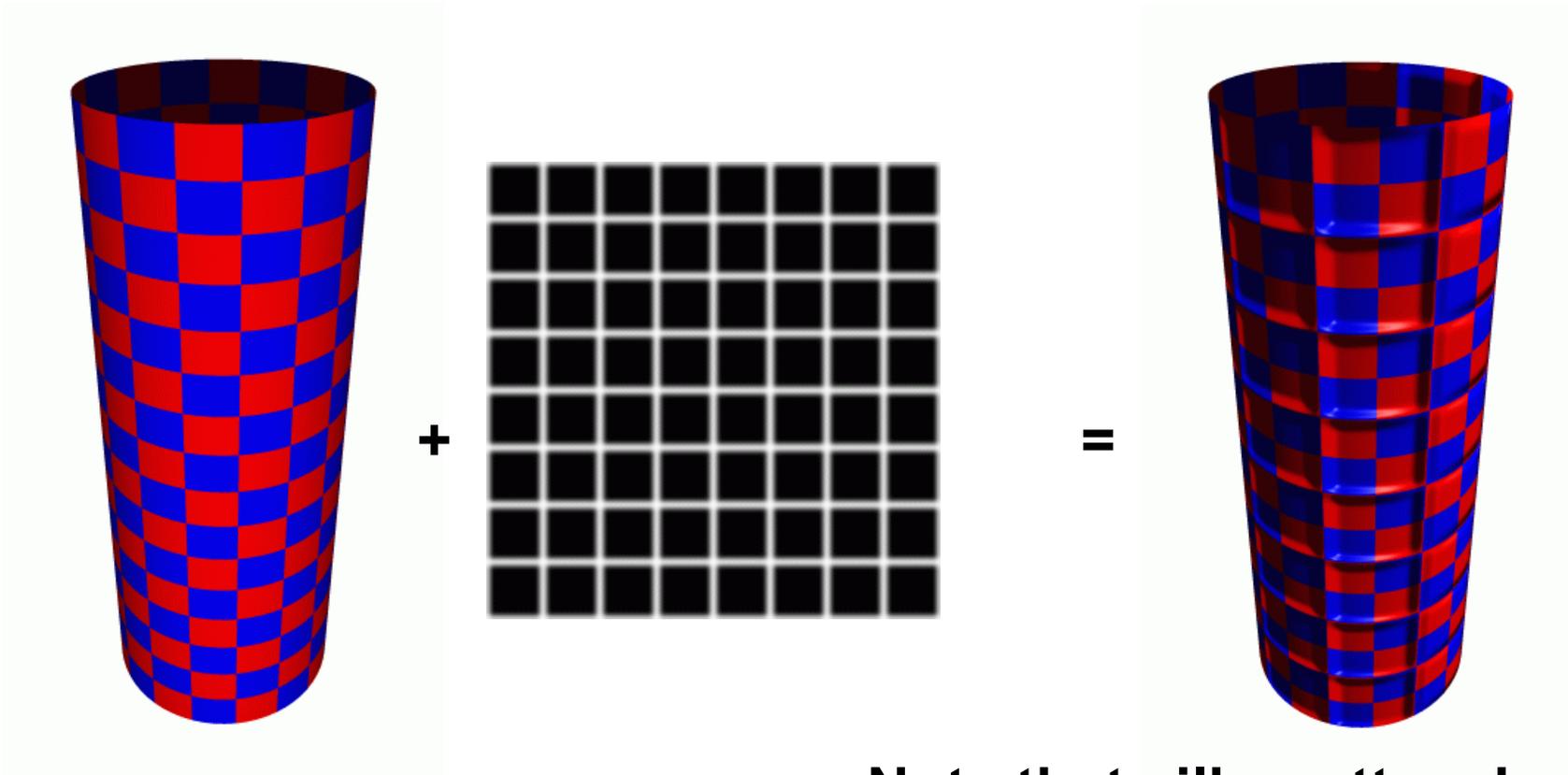
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- **Modifies the normal not the actual geometry**
  - **Texture treated as a heightfield**
  - **Partial derivatives used to change the normal**
  - **Causes surface to appear deformed by the heightfield**



# More Bump Map Examples

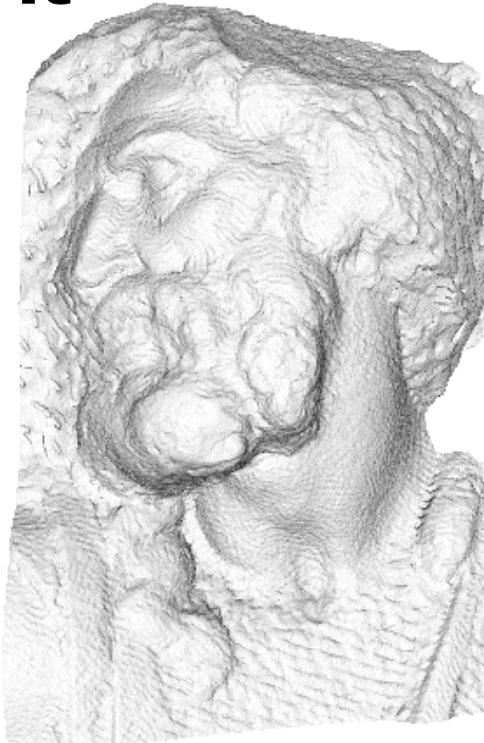
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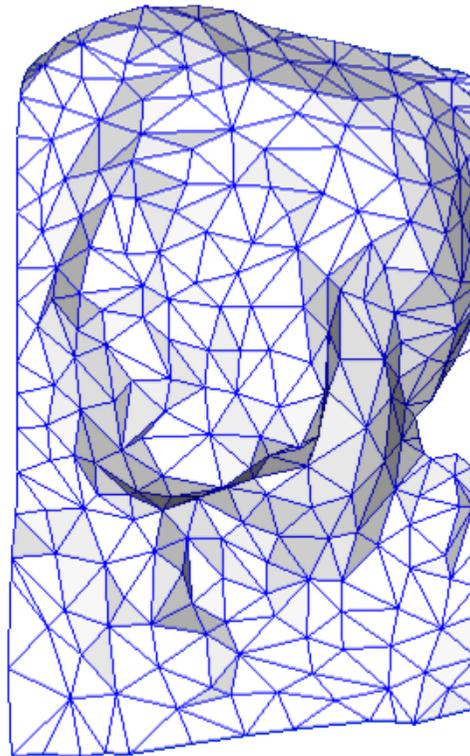
**Note that silhouette edge of the object not affected!**

# Normal Mapping

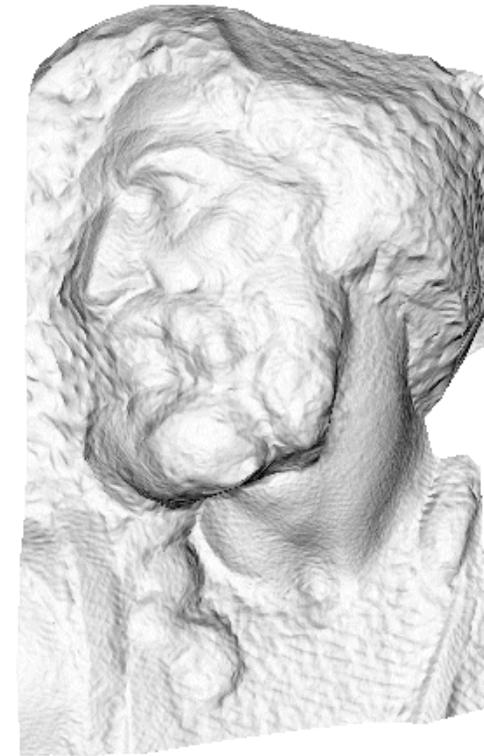
- Replaces the normal rather than tweaking it



original mesh  
4M triangles



simplified mesh  
500 triangles



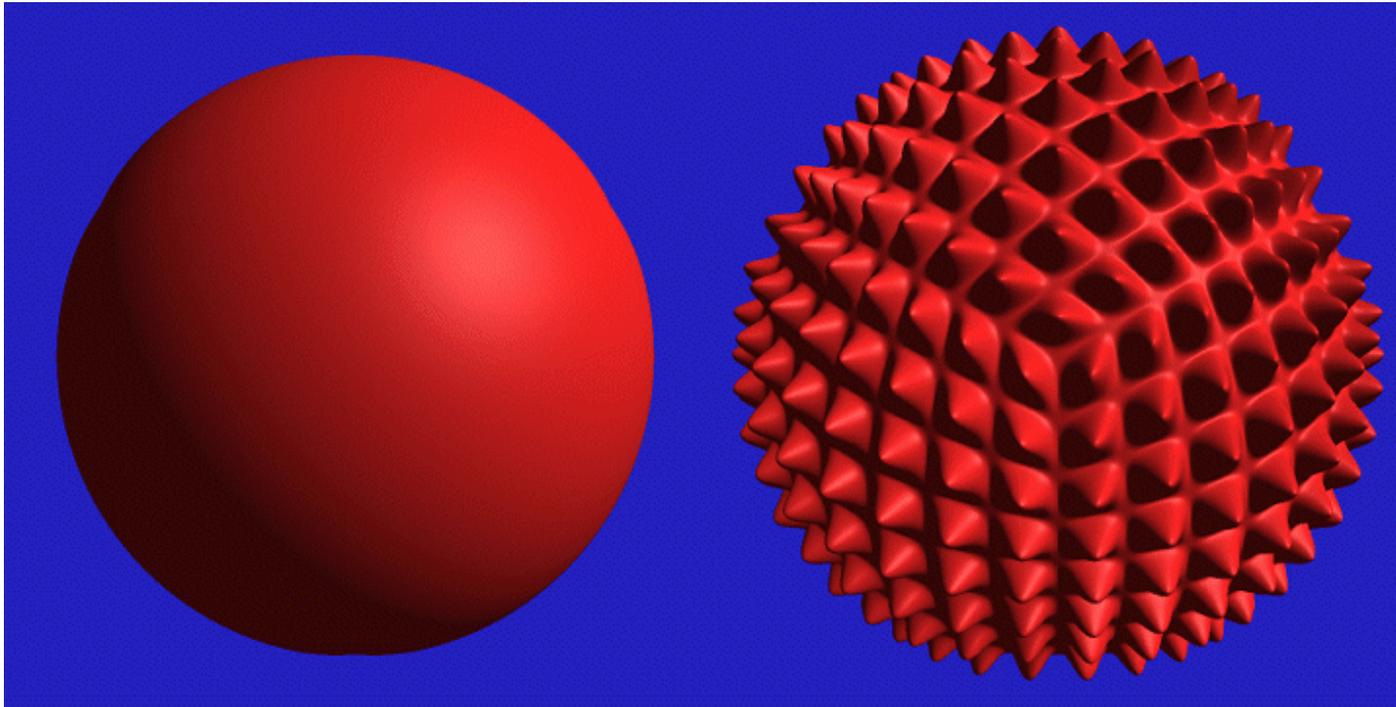
simplified mesh  
and normal mapping  
500 triangles



# Displacement Mapping

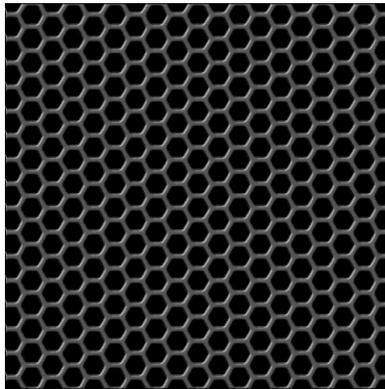
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- **Texture maps can be used to actually move surface points**

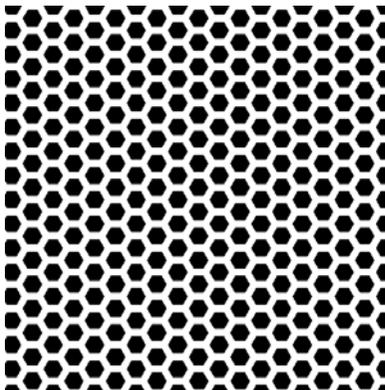


# Opacity Maps

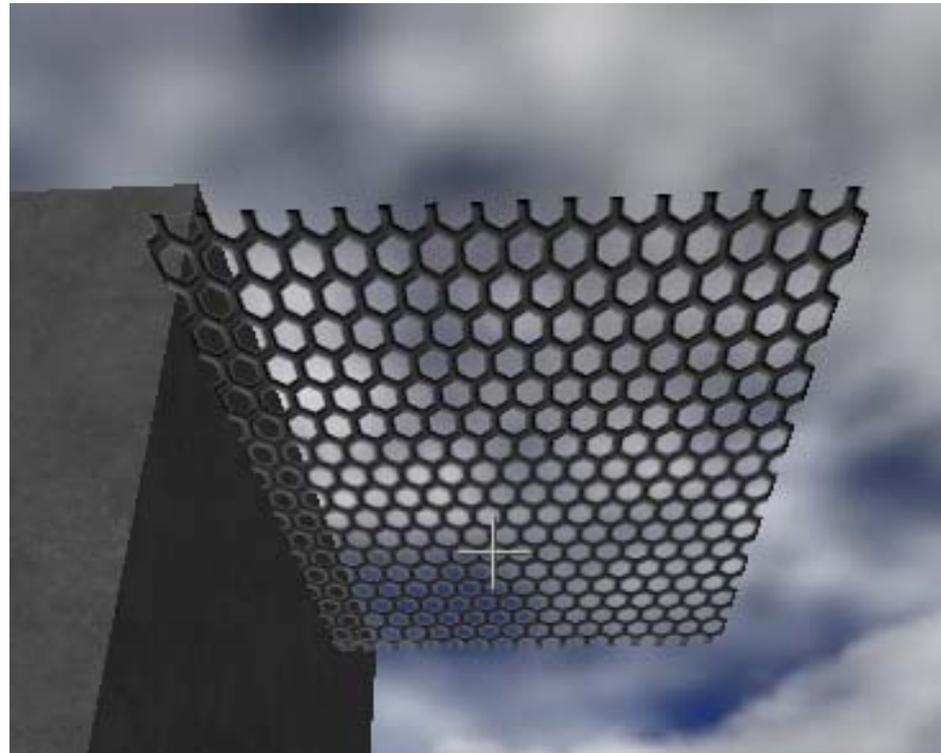
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RGB channels



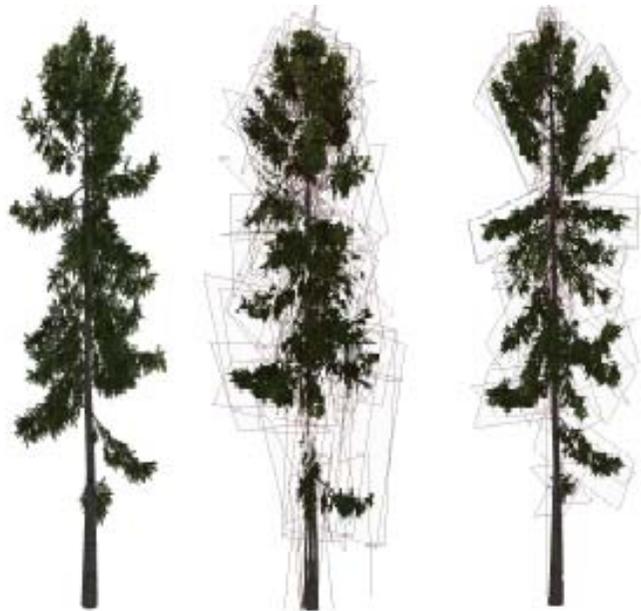
alpha channel



Use the alpha channel to make portions of the texture transparent

# Billboards

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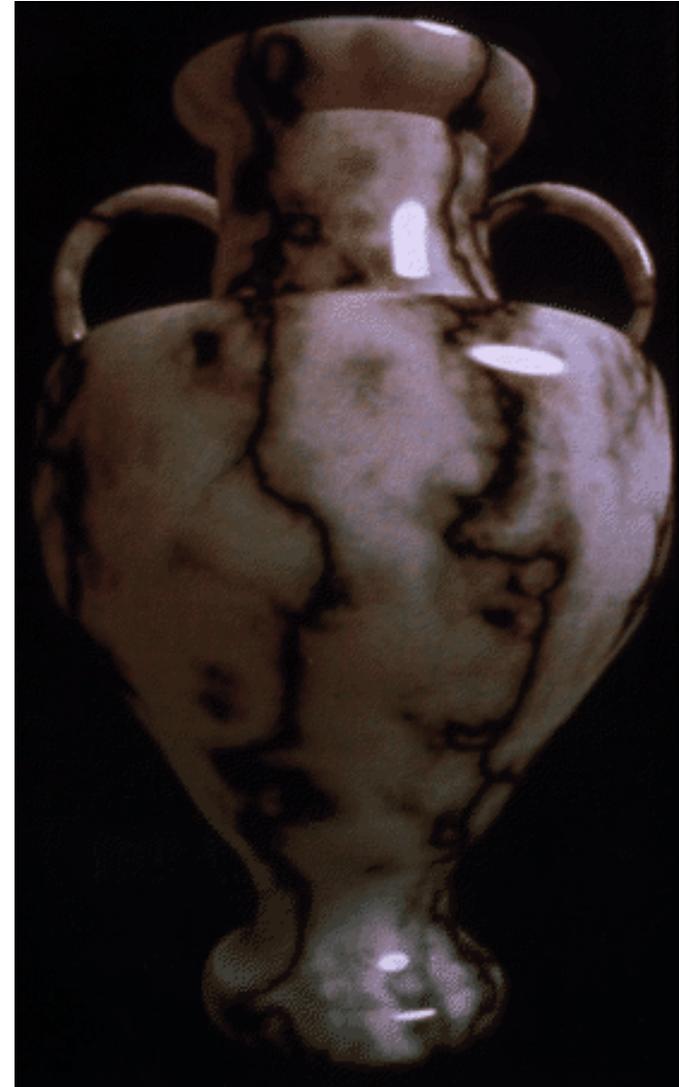


Replace complex geometry with polygons  
texture mapped with transparent textures

# 3D or Solid Textures

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- **Solid textures are three dimensional assigning values to points in 3 space**
  - **Very effective at representing some types of materials such as marble and wood**
- **Generally, solid textures are defined procedural functions rather than tabularized functions as used in 2D**



# Class Objectives were:

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- **Texture mapping overview**
- **Texture filtering**
- **Various applications of texture mapping**

# Next Time

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- **Visibility and ray tracing**

# Homework

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- **Go over the next lecture slides before the class**
- **No more video abstract submissions on June**