CS380: Computer Graphics Viewing Transformation

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Class Objectives

- Know camera setup parameters
- Understand viewing and projection processes
- Related to Ch. 4: Camera Setting
- At the last class:
 - Briefly went over rendering pipeline
 - 3D rotation w/ the frame concept
 - Geometric meanings of dot product and cross products



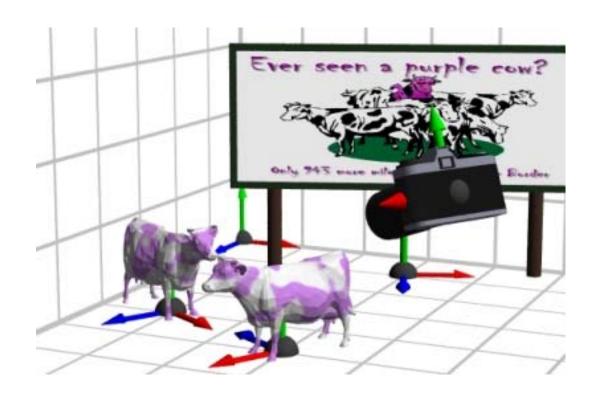
Questions

• In rendering pipeline, it seems to me that the Trivial rejection in Modeling Transforms and Clipping do the same function. Eliminating not visible things. What is the difference between them?



Viewing Transformations

- Map points from world spaces to eye space
 - Can be composed from rotations and translations





Viewing Transformations

- Goal: specify position and orientation of our camera
 - Defines a coordinate frame for eye space

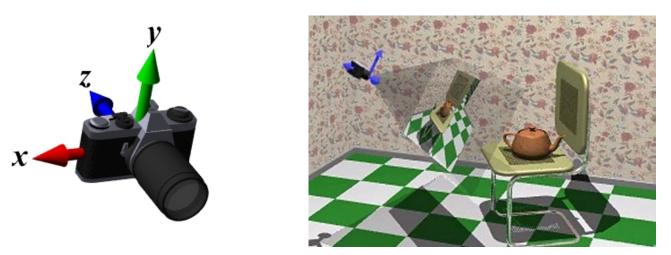




"Framing" the Picture

• A new camera coordinate

- Camera position at the origin
- Z-axis aligned with the view direction
- Y-axis aligned with the up direction

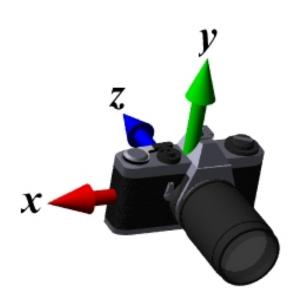


 More natural to think of camera as an object positioned in the world frame



Viewing Steps

 Rotate to align the two coordinate frames and, then, translate to move world space origin to camera's origin







An Intuitive Specification

• Specify three quantities:

- the image
- Eye point (e) position of the camera
 - Look-at point (p) center of the image
- Up-vector (\vec{u}_a) will be oriented upwards in





Deriving the Viewing Transformation

- First compute the look-at vector and normalize $\vec{l} = p - e$ $\hat{l} = \frac{\vec{l}}{|\vec{l}|}$
- Compute right vector and normalize

 $\vec{r} = \vec{l} \times \vec{u}_a$ $\hat{r} = \frac{\vec{r}}{|\vec{r}|}$

• Perpendicular to the look-at and up vectors

- Adjust up-vector
 - \vec{u}_a is only approximate direction
 - Perpendicular to right and look-at vectors

$$\hat{\mathbf{u}} = \hat{\mathbf{r}} \times \hat{\mathbf{l}}$$



Our Approach

 Translate the camera origin to the world origin, followed by rotating the camera coordinates (E) to the world coordinate (W):

$$Wc = ER_v T_{-e}c$$



Rotation Component

Map our vectors to the cartesian coordinate axes

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} \hat{r} & \hat{u} & -\hat{j} \end{bmatrix} R_{v}$$

• To compute R_v we invert the matrix on the right

 This matrix M is orthonormal (or orthogonal) – its rows are orthonormal basis vectors: vectors mutually orthogonal and of unit length

• Then,
$$M^{-1} = M^T$$

• So, $\mathbf{R}_v = \begin{bmatrix} \hat{r}^t \\ \hat{u}^t \\ -\hat{\mathbf{j}}^t \end{bmatrix}$



Translation Component

- Need to translate all world-space coordinates so that the eye point is at the origin
- Composing these transformations gives our viewing transform, V

$$\dot{w}^t = \dot{e}^t \mathbf{R}_v \mathbf{T}_{-\dot{e}}$$

$$\mathbf{V} = \mathbf{R}_{v}\mathbf{T}_{-\dot{e}} = \begin{bmatrix} \hat{r}_{x} & \hat{r}_{y} & \hat{r}_{z} & 0\\ \hat{u}_{x} & \hat{u}_{y} & \hat{u}_{z} & 0\\ -\hat{l}_{x} & -\hat{l}_{y} & -\hat{l}_{z} & 0\\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & -e_{x}\\ 0 & 1 & 0 & -e_{y}\\ 0 & 0 & 1 & -e_{z}\\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} \hat{r} & -\hat{r} \cdot \vec{e}\\ \hat{u} & -\hat{u} \cdot \vec{e}\\ -\hat{l} & \hat{l} \cdot \vec{e}\\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Transform a world-space point into a point in the eye-space

Viewing Transform in OpenGL

OpenGL utility (glu) library provides a viewing transformation function:

gluLookAt (double eyex, double eyey, double eyez, double centerx, double centery, double centerz, double upx, double upy, double upz)

 Computes the same transformation that we derived and composes it with the current matrix

Same to glm::gtc::matrix_transform::lookAt (..)



Example in the Skeleton Codes of PA2

```
void setCamera ()
{ ...
// initialize camera frame transforms
  for (i=0; i < cameraCount; i++ )
   double* c = cameras[i];
   wld2cam.push_back(FrameXform());
   glPushMatrix();
   glLoadldentity();
   gluLookAt(c[0],c[1],c[2], c[3],c[4],c[5], c[6],c[7],c[8]);
   glGetDoublev( GL_MODELVIEW_MATRIX, wld2cam[i].matrix() );
   glPopMatrix();
   cam2wld.push_back(wld2cam[i].inverse());
```

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Projections

Map 3D points in eye space to 2D points in image space



- Two common methods
 - Orthographic projection
 - Perspective projection



Orthographic Projection

- Projects points along lines parallel to z-axis
 - Also called parallel projection
 - Used for top and side views in drafting and modeling applications
- Appears unnatural due to lack of perspective foreshortening

Notice that the parallel lines of the tiled floor remain parallel after orthographic projection!



Orthographic Projection

 The projection matrix for orthographic projection is very simple

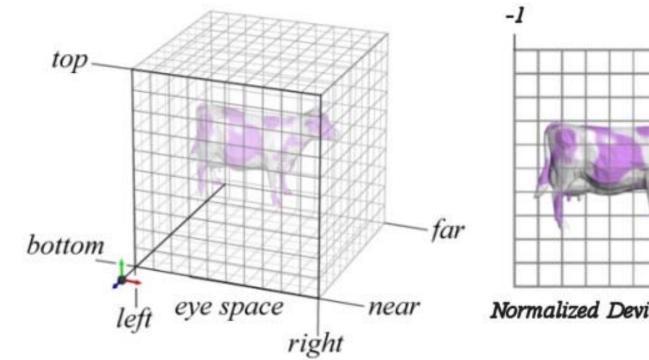
$$\begin{bmatrix} \mathbf{x}' \\ \mathbf{y}' \\ \mathbf{z}' \\ \mathbf{1} \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \mathbf{x} \\ \mathbf{y} \\ \mathbf{z} \\ \mathbf{z} \\ \mathbf{1} \end{bmatrix}$$

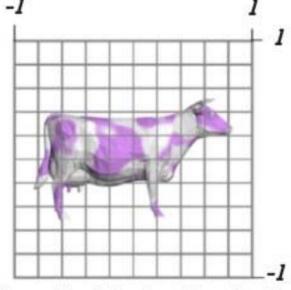
Next step is to convert points to NDC



View Volume and Normalized **Device Coordinates**

- Define a view volume
- Compose projection with a scale and a translation that maps eye coordinates to normalized device coordinates

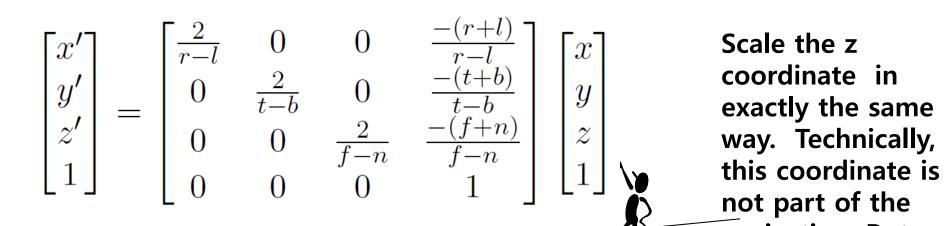




Normalized Device Coordinates



Orthographic Projections to NDC



Some sanity checks:

not part of the projection. But, we will use this value of z for other purposes

$$x'(l) = \frac{2l}{r-l} - \frac{r+l}{r-l} = -\frac{r-l}{r-l} = -1$$



Orthographic Projection in OpenGL

This matrix is constructed by the following OpenGL call:

void glOrtho(double left, double right, double bottom, double top, double near, double far);

Same to glm::gtc::matrix_transform::ortho (..)



Perspective Projection

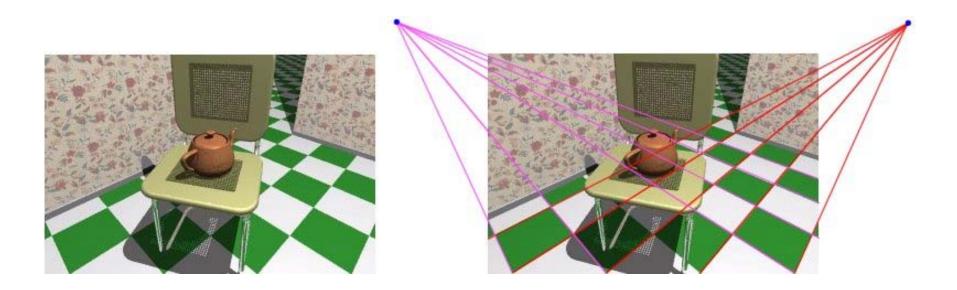
- Artists (Donatello, Brunelleschi, Durer, and Da Vinci) during the renaissance discovered the importance of perspective for making images appear realistic
- Perspective causes objects nearer to the viewer to appear larger than the same object would appear farther away
- Homogenous coordinates allow perspective projections using linear operators





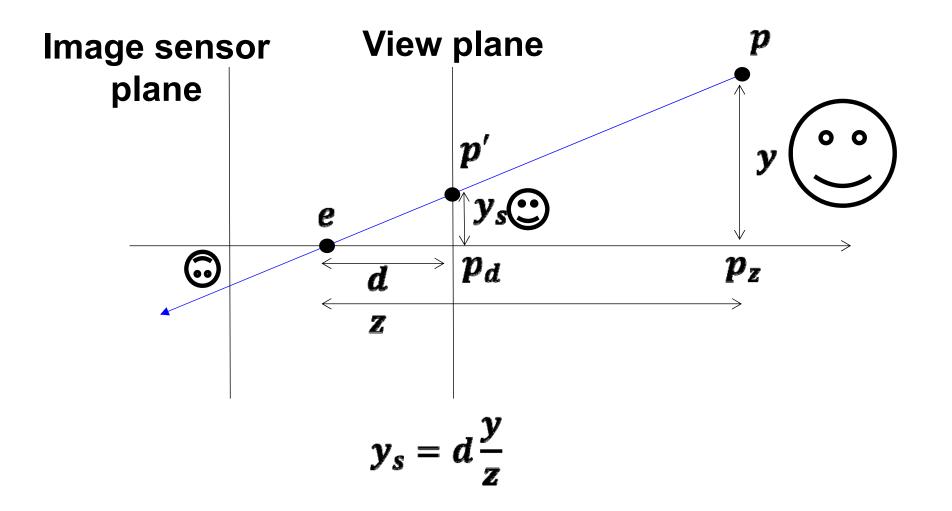
Signs of Perspective

Lines in projective space always intersect at a point





Perspective Projection for a Pinhole Camera





Perspective Projection Matrix

• The simplest transform for perspective projection is:

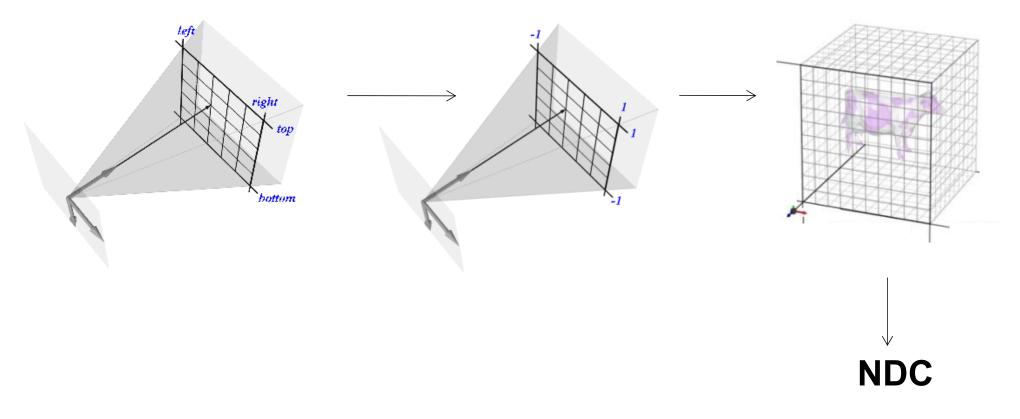
$$\begin{bmatrix} wx' \\ wy' \\ wz' \\ w \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

- We divide by w to make the fourth coordinate 1
 - In this example, w = z
 - Therefore, x' = x / z, y' = y / z, z' = 0



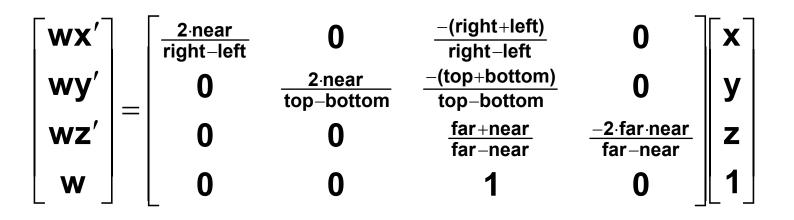
Normalized Perspective

As in the orthographic case, we map to normalized device coordinates





NDC Perspective Matrix

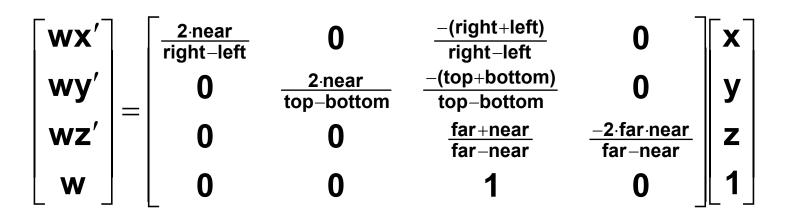


 The values of left, right, top, and bottom are specified at the near depth. Let's try some sanity checks:

$$\begin{aligned} x &= left\\ z &= near \Rightarrow x' = \frac{\frac{2 \cdot near \cdot left}{right - left} - \frac{near(right + left)}{right - left}}{near} = \frac{-near}{near} = -1\\ x &= right\\ z &= near \Rightarrow x' = \frac{\frac{2 \cdot near \cdot right}{right - left} - \frac{near(right + left)}{right - left}}{near} = \frac{near}{near} = 1 \end{aligned}$$



NDC Perspective Matrix



 The values of left, right, top, and bottom are specified at the near depth. Let's try some sanity checks:

$$z = far \Rightarrow z' = \frac{far \frac{far + near}{far - near} + \frac{-2 \cdot far \cdot near}{far - near}}{far}}{far} = \frac{\frac{far(far - near)}{far - near}}{far}}{far} = 1$$

$$z = near \Rightarrow z' = \frac{near \frac{far + near}{far - near} + \frac{-2 \cdot far \cdot near}{far - near}}{near}}{near} = \frac{\frac{near(near - far)}{far - near}}{near}}{near} = -1$$



Perspective in OpenGL

 OpenGL provides the following function to define perspective transformations:

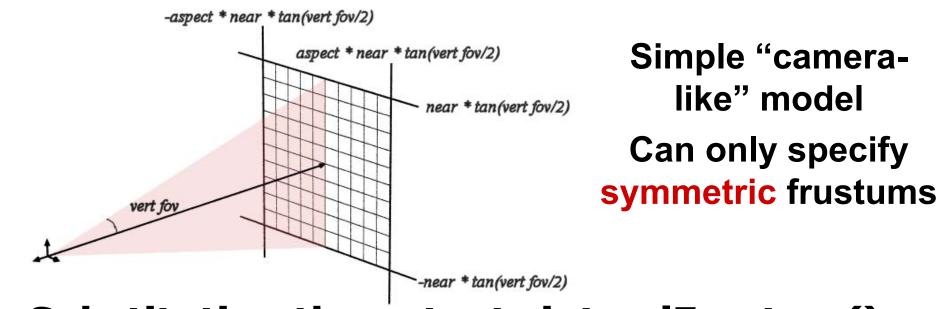
> void glFrustum(double *left*, double *right*, double *bottom*, double *top*, double *near*, double *far*);

 Some think that using glFrustum() is nonintuitive.
 So OpenGL provides a function with simpler, but less general capabilities

void gluPerspective(double *vertfov*, double *aspect*, double *near*, double *far*);



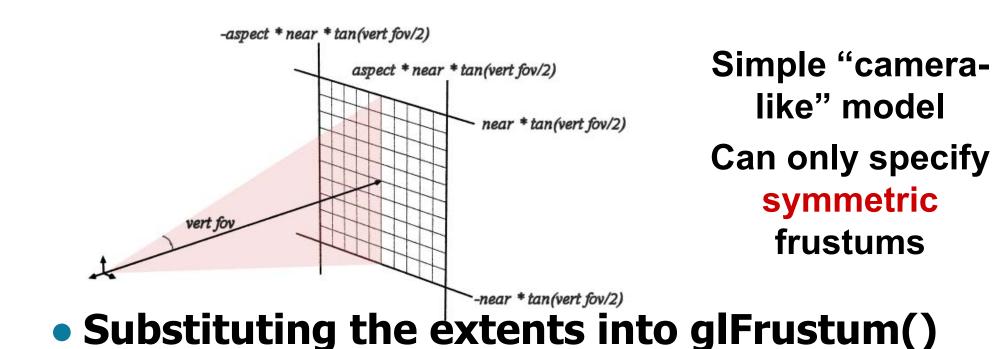
gluPerspective()

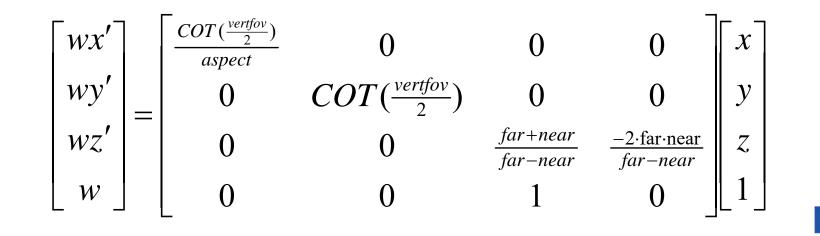


Substituting the extents into glFrustum()



gluPerspective()





Example in the Skeleton Codes of PA2

```
void reshape( int w, int h)
{
    width = w; height = h;
    glViewport(0, 0, width, height);

    glMatrixMode(GL_PROJECTION);
    glLoadIdentity();

    // Define perspective projection frustum
    double aspect = width/double(height);

    gluPerspective(45, aspect, 1, 1024);
```

glMatrixMode(GL_MODELVIEW);

glLoadIdentity();

// Select The Projection Matrix
// Reset The Projection Matrix

// Select The Modelview Matrix

// Reset The Modelview Matrix



Class Objectives were:

- Know camera setup parameters
- Understand viewing and projection processes
- Related to Ch. 4: Camera Setting



Homework

- Watch SIGGRAPH Videos
- Go over the next lecture slides



PA3



- PA2: perform the transformation at the modeling space
- PA3: perform the transformation at the viewing space



Next Time

Interaction



figs







