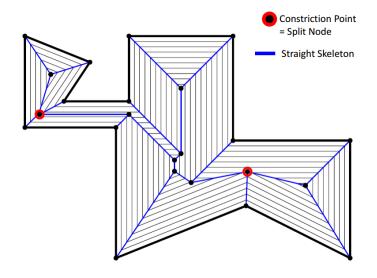
Real-Time 3D Navigation for Autonomous Vision-Guided MAVs

Seungwon Song

2017.05.23 CS686 Paper Presentation #2

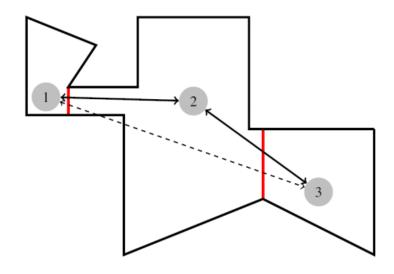


Suzi Kim's Presentation



Cell Decomposition

- Shrink
 - Split



Cell Visit Using TSP



Contents

- Introduction
- Conventional approach
- Basic concepts
- Detail of each concepts
- Result



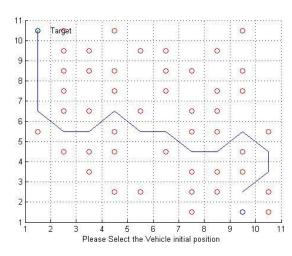
Introduction

- Regular 3D state lattice requires a large amount of memory while graph search even though problem is easier to solve.
- Using Octree-based state lattice which represent discretizes large swathes of free space into few symbolic octants.
- Warning!
 - It does not contain any Math, just in robotical perspective!
 - So, just basic result comparison with conventional method.

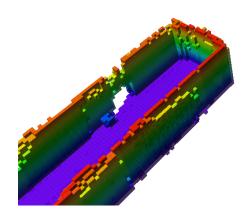


Conventional Approach

- There are several grid-based path planning method in 2D.
- In 3D, there are too many points, so reduced them by using Octomap.
- Using reduced 3D grid, Researchers can use conventional A* or other algorithms



Grid based pathplanning



Octomap

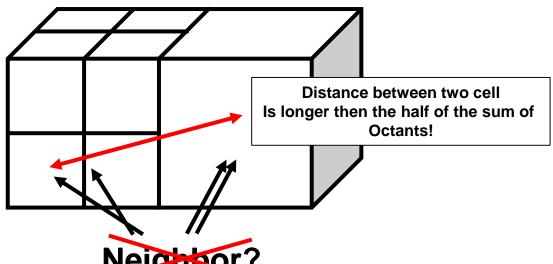


Basic Concepts

- Simplify Quadrotor dynamic
- Reduce resolution of Octomap (octants)
- Octree-Based State Lattice
 - Adjacency between octree node states
 - Multi-resolution path lookup-table
 - Pre-discretization
- Local 3D State Lattice
- Graph search
 - Optimal path finding
 - Path reconstruction



- Adjacency between octree node states
 - To determine whether two octants are adjacent to each other.
 - If distance between two cell's center exceeds half of the sum of two octants' cell size, two octants are not adjacent.

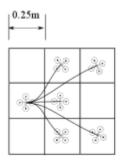


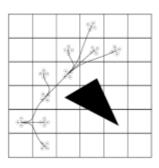
Algorithm 1 Algorithm to find neighbors for each of a *node*'s children when the node is split.

```
1: if node is no longer a leaf due to updated map informa-
      Split node into eight children (child[i], i \in \{1, 2, ..., 8\})
      for i = 1 \rightarrow 8 do
         child-node = child[i]
         add the child-node's brothers (child[j], j \neq i, j \in
         1, 2, \dots 8) as neighbors
6:
         for each neighbor of node, neighbor[k] do
7:
           if neighbor[k] is still the neighbor of child-node
           after the split then
              add neighbor [k] as the neighbor of child-node
8:
           end if
         end for
      end for
12: end if
```



- Multi-resolution path lookup-table
 - Computing path between every octants' consume much computational cost.
 - How about save all pre-computed cost and path in the table?
 - They set 16 states in yaw angle (22.5 deg inc)
 - They set lookup index $(\theta_1,x_1-x_2,y_1-y_2,z_1-z_2,\theta_2)$





Algorithm 2 Multi-resolution path lookup-table construction.

```
1: for i = 1 \to 16, x = -N \to N, y = -N \to N,
    z = -N \rightarrow N, j = 1 \rightarrow 16 do
 2: LUT_COST[i][x][y][z][j] = infinity
      LUT_PATH[i][x][y][z][j] = undefined
 5: for i = 1 \rightarrow 16 do
      for every state v in the state lattice do
         dist[v] := infinity
         previous[v] := undefined
      end for
      Q := \text{empty priority queue}
      s\_start := the origin of the lattice with an orientation
      dist[s\_start] = 0
      insert s_start into Q
      while Q is not empty do
         u := \text{vertex in } Q \text{ with minimum } \text{dist}[u]
16:
         remove u from Q
17:
         for each neighbor v of u do
           i := the orientation index of v
18:
           (dx, dy, dz) := the 3D coordinate difference
19:
           between u and v
           checkdist := dist[u] + cost(u,v)
20:
           if checkdist < dist[v] then
21:
              dist[v] := checkdist
              previous[v] := u
             LUT_COST[i][dx][dy][dz][j] = checkdist
25:
              waypoint = v
              clear LUT_PATH[i][dx][dy][dz][j]
27:
              while waypoint \neq s\_start do
28:
                            back
                                        waypoint
                LUT_PATH[i][dx][dy][dz][j]
                waypoint = previous[waypoint]
              end while
           end if
31:
         end for
      end while
34: end for
```



- Multi-resolution path lookup-table
 - But save all computation result consume lots of memory!
 - They just consider 'distance' as cost.
 - So, $(0,0,0,\theta_1)$ to (x,y,z,θ_2) can be reflected to $(0,0,0,\theta_1)$ to $(x,y,-z,\theta_2)$!
 - Also, all 16 possible θ_1 can be reduced to 0,22.5,45 degrees.
 - So, they say memory requirement reduced by 90%

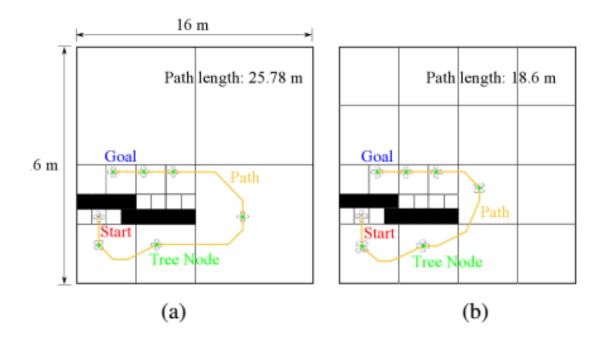
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        u := \text{vertex in } Q \text{ with minimum } \text{dist}[u]
16:
        remove u from Q
        for each neighbor v of u do
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          j := the orientation index of v
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           checkdist := dist[u] + cost(u,v)
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          if checkdist < dist[v] then
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22:
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             LUT\_COST[i][dx][dy][dz][j] = checkdist
              waypoint = v
             clear LUT_PATH[i][dx][dx][dz][j]
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31:
        end for
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```



Pre-discretization

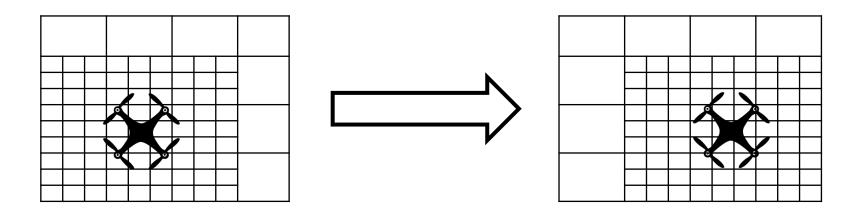
- Octree-based state lattice may compute highly suboptimal path.
- More octree level means large pre-computed cost and path table.
- So they enforce a minimum octree level on all leaf node.





Local 3D State Lattice

- Path planning is critical especially for obstacle avoidance.
- They make local high-resolution state lattice centered on the MAV.



- These method can maintain octree-based graph structure.
- Can help the MAV navigate around nearby obstacles.



Graph Search

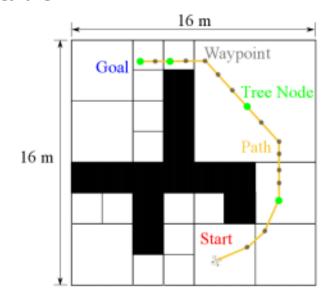
Optimal Path Finding

- Use simple A* graph search algorithm. (Using the method above, any A* based algorithm can be used)
- A* algorithm heavily depends on the quality of the heuristic function.
 - They applied holonomic-with-obstacles heuristic [1]
 - Ignores the non-holonomic nature of robot, and then make 2D path with obstacle map
 - 3D space into 2D space by $f_2(x, y) = \min_{\theta} f_3(x, y, \theta)$, which means that 2D state is assumed to be safe (no collision) if there exists at least one safe 3D state with same 2D projection.
 - •They reduced candidate states, so A* able to find the best path in short time.

Graph Search

Path reconstruction

- Path obtained by A* is actually a series of high-resolution primitive motion.
- They look up the path decompositions in the multiresolution lookup table.



Green dot: Node achieved by A* Grey dot: actual waypoints Clay line: final full path



Result

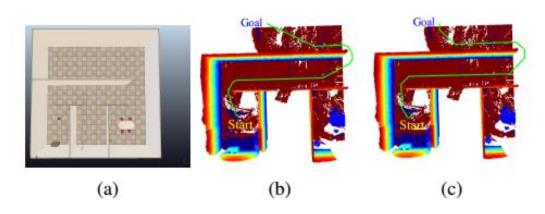
- Time & Memory usage reduce
 - For 50 different goals with maximum resolution of 0.25m
 - Compare with regular-state-lattice-based path planner.

TABLE I: Statistical Results from Simulation Experiments.

	Our Path Planner	Baseline Path Planner
Map Update Time ¹ (s)	0.0991	0.0185
Graph Search Time ² (s)	0.299	10.1803
Heuristics Time ³ (s)	0.0288	0.0288
Total Time (s)	0.428	10.23
Total Path Length (m)	1108.32	1009.21
Optimality Ratio	1.11	1
Memory Usage (Gb)	0.474	1.39

¹ the time taken to update obstacle information and construct graph

³ the time taken to compute heuristics





² the time taken to run A* algorithm on the given graph

Result

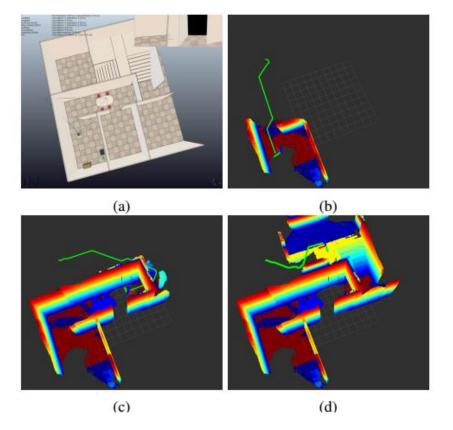
Unknown Environment

A : Entire Environment

B : Initial Search to goal

C: UAV goes through Stairs

D : Successfully find path

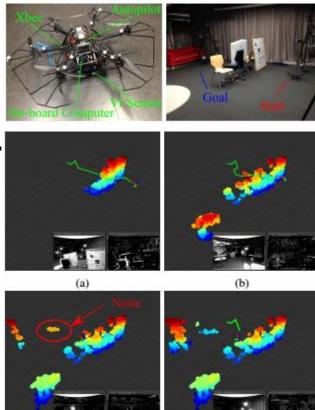




Result

Real Environment

- Also in real environment, Algorithm works well.
- UAV found obstacle, and planned path.





ANY QUESTION?

